

James F.W. Purdom CIRA, Colorado State University Chair, AOMSUC ICSC

Vorticity Equation: From the AMS Glossary of Meteorology

The vorticity equation takes on slightly different forms depending on whether height or pressure is taken as the vertical coordinate. With height as the vertical coordinate, and with friction terms omitted, the vertical component of the vorticity equation is

$$\frac{D\zeta}{Dt} = -(\zeta + f)\left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y}\right) - \frac{2\Omega\cos\phi}{a}v$$
$$+ \left(\frac{\partial w}{\partial y}\frac{\partial u}{\partial z} - \frac{\partial w}{\partial x}\frac{\partial v}{\partial z}\right) + \left(\frac{\partial p}{\partial x}\frac{\partial \alpha}{\partial y} - \frac{\partial p}{\partial y}\frac{\partial \alpha}{\partial x}\right)$$

where ζ is the vertical component of the relative vorticity; *f* the Coriolis parameter; *u*, *v*, and *w* the components of the wind velocity toward the east (*x*), north (*y*), and vertical (*z*); Ω the angular speed of the earth; *p* and α the air pressure and specific volume, respectively; *a* the earth's radius; and φ the latitude. The left-hand member of the equation represents the material rate of change of the relative vorticity of an air parcel. The first term on the right describes the effect of horizontal divergence. The second term on the right is the Rossby parameter times *v* and represents the change in vorticity resulting from latitudinal displacement. The third term on the right, often called the vertical shear, twisting, or tilting term, describes the influence of a horizontal gradient of vertical velocity in transforming vorticity about a horizontal axis to that about a vertical axis. The last term represents the generation of vorticity by pressure–volume solenoids. When pressure is taken as the vertical coordinate, and all differentiations are performed on an isobaric surface, the equation is simplified by the absence of the solenoidal term:

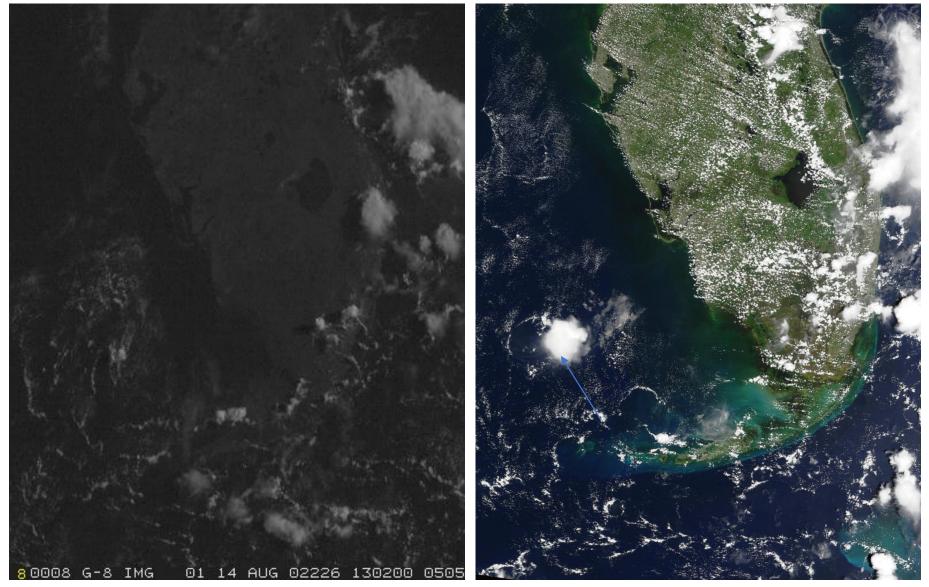
Organized circulation Vorticity - On the local scale

- Convergence on preexisting vorticity
- Tilting of vorticity from one plane to another
- Advection from one place to another
- Differential heating (does not require pre-existing vorticity)
- Friction

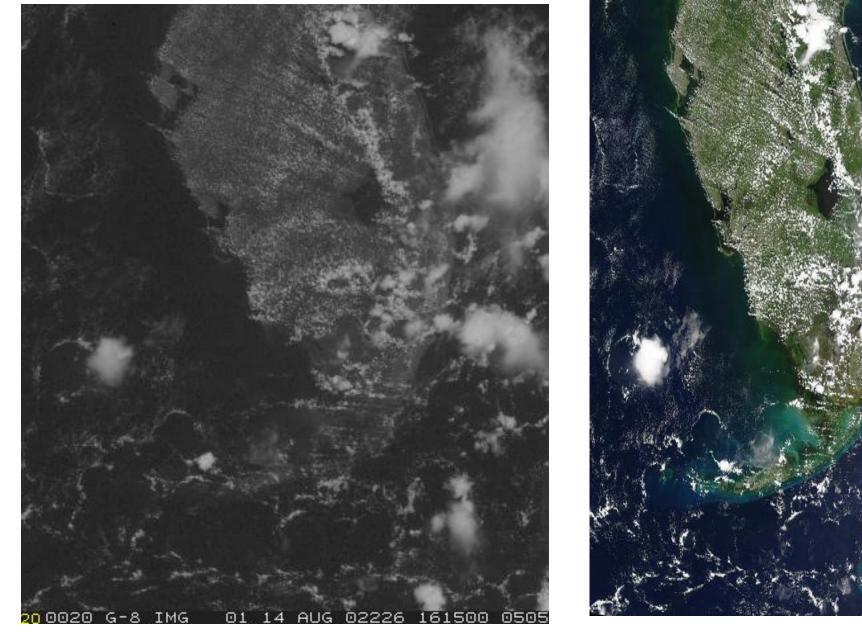
Differential heating examples

- When one thinks of differential heating the land sea breeze phenomena immediately comes to mind.
- Another differential heating mechanism is the thunderstorm itself: through evaporation of rain cooled air a differential heating is developed in a quick and often dramatic fashion.

Observing the process (geostationary) can help analyze polar imagery.



GOES-8 loop from 1033 to 1615 (left) and MODIS true color image near 1615 (right). While noting the convection over land, pay attention to convection over the ocean.



GOES-8 loop, 1615-2332, and MODIS true color image near 1615 (right). While noting the convection over land, pay exceptional attention to convection over the ocean.

GOES-9 GOES-9 (NASA-GSFC

Rapid-scan test 8 am - 8 pm EDT July 2, 1995

South Florida

July 13th edition

1995 Jul 2 12:11 UTC

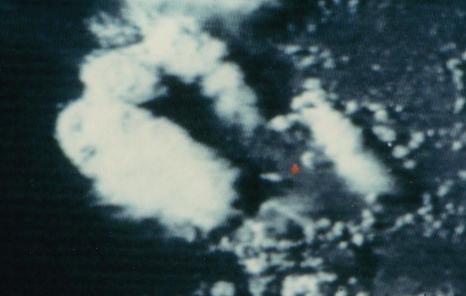
Animation of one minute GOES imagery illustrating the role of storm outflow in generating new convection.

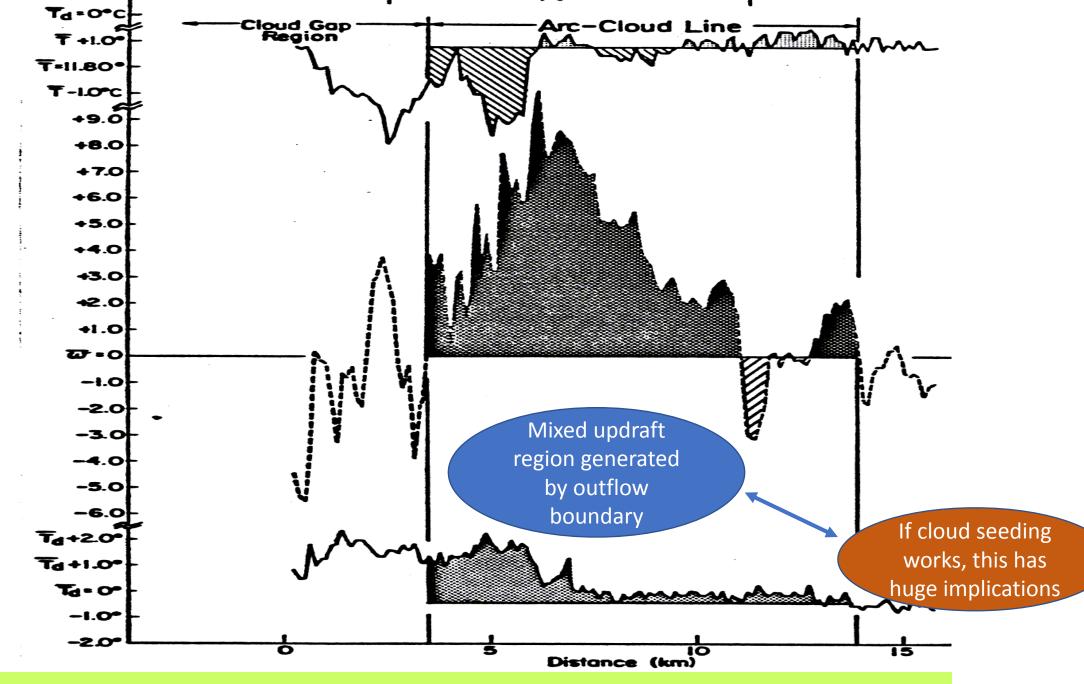
A flight through an arc cloud line



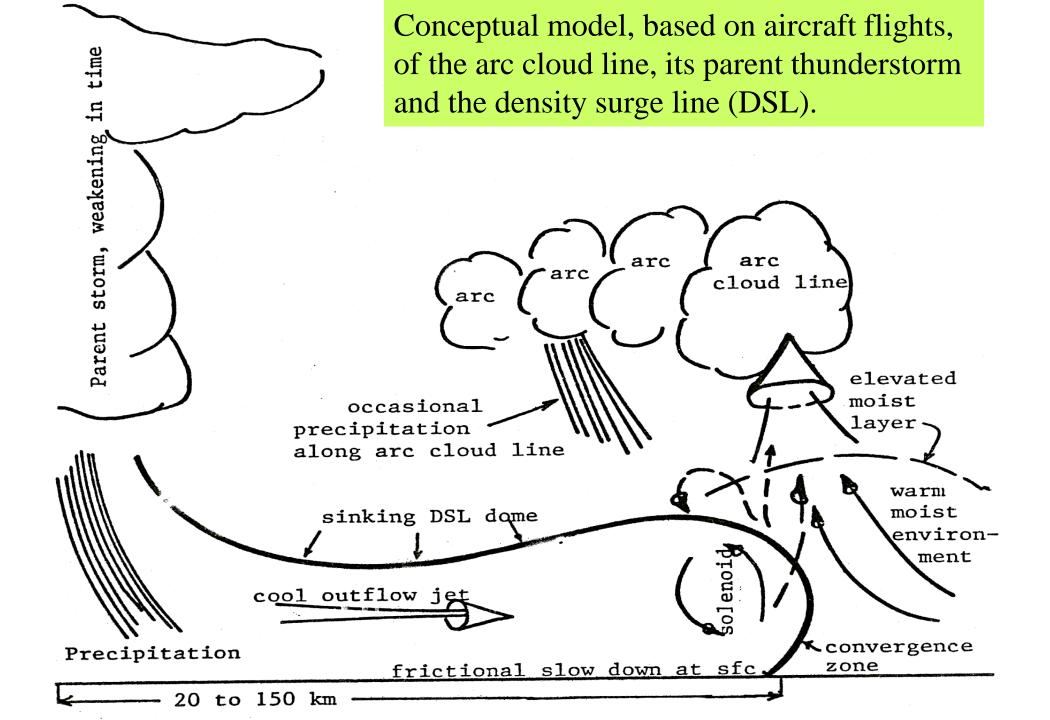


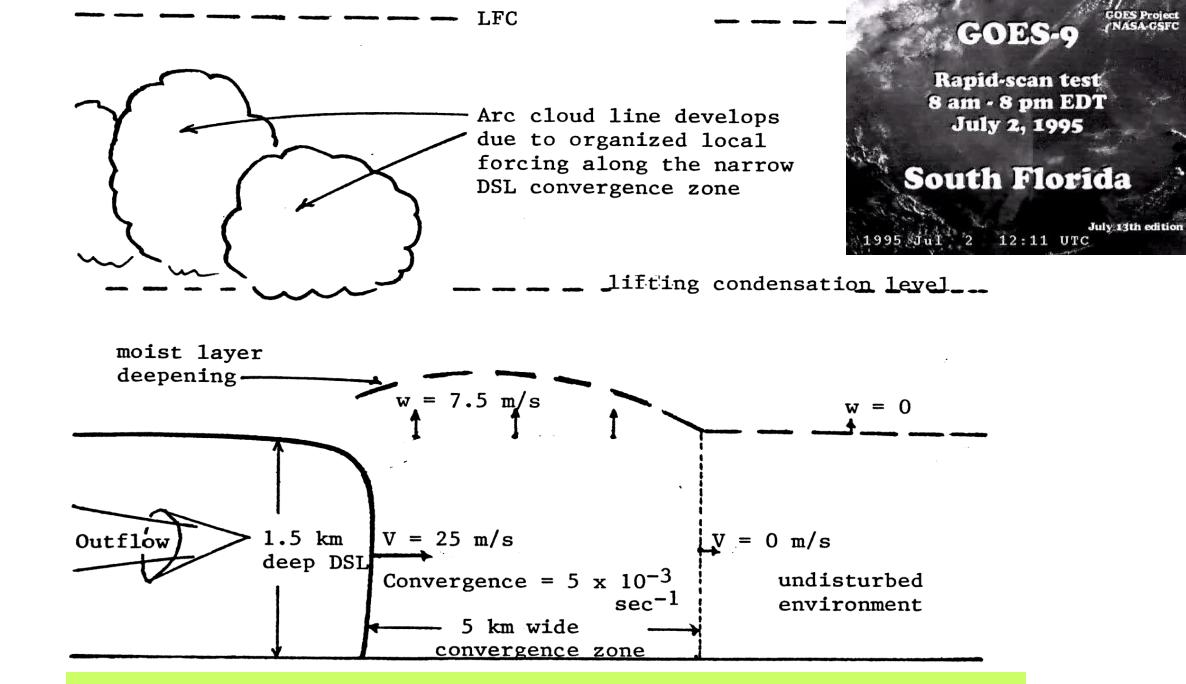




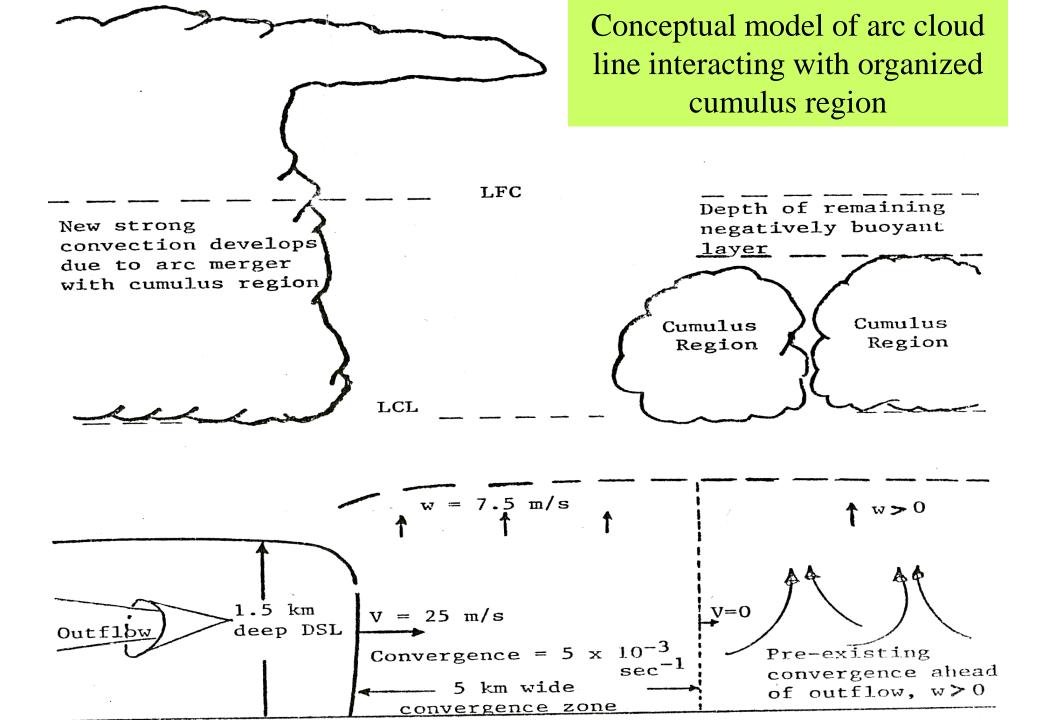


Aircraft data from penetration of an intense arc cloud's sub-cloud region





Convergence and vertical motion region associated with the arc cloud



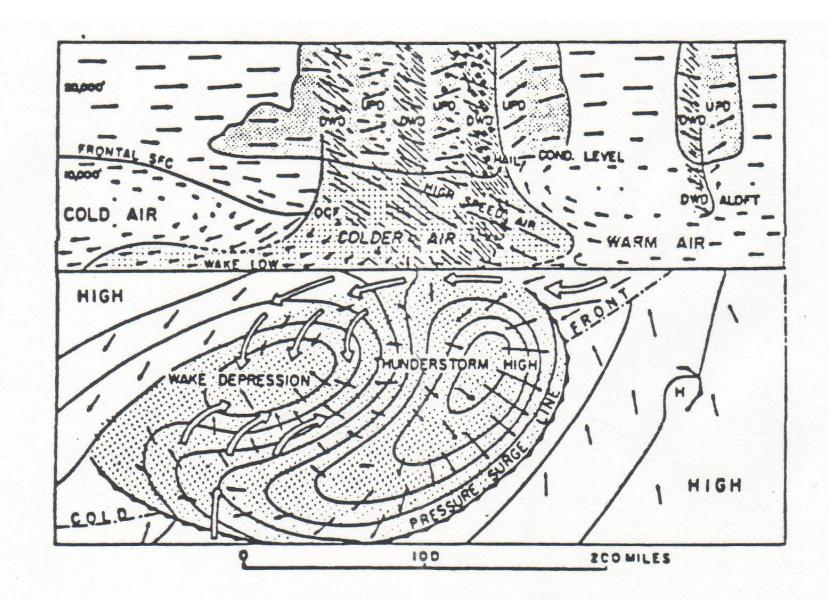


Figure . From Fujita (1955) illustrating the importance of raincooled air in the production of the mesoscale high pressure system.

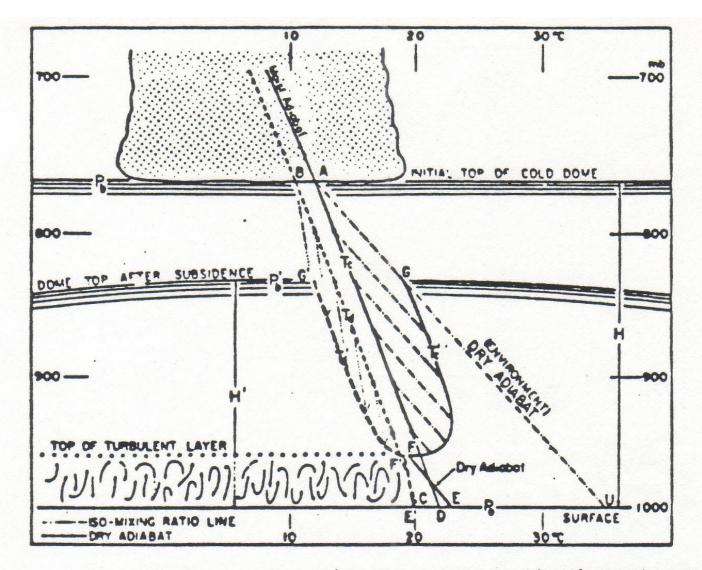
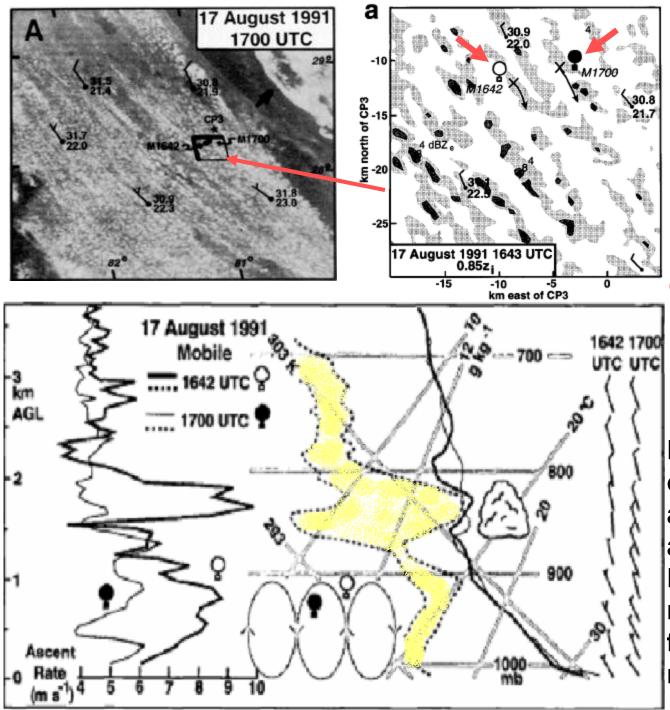


Figure . From Fujita (1959) illustrating the importance of subsidence within the cold dome, after the passage of the thunderstorm system, which leads to clearing in that region.



The moisture available to support deep convection can vary dramatically over very short distances as the convective **boundary layer** develops.

Left about 2 g/kg over a distance of about 10 km (from a study over Florida , based on research aircraft flights and special rawinsonde data).

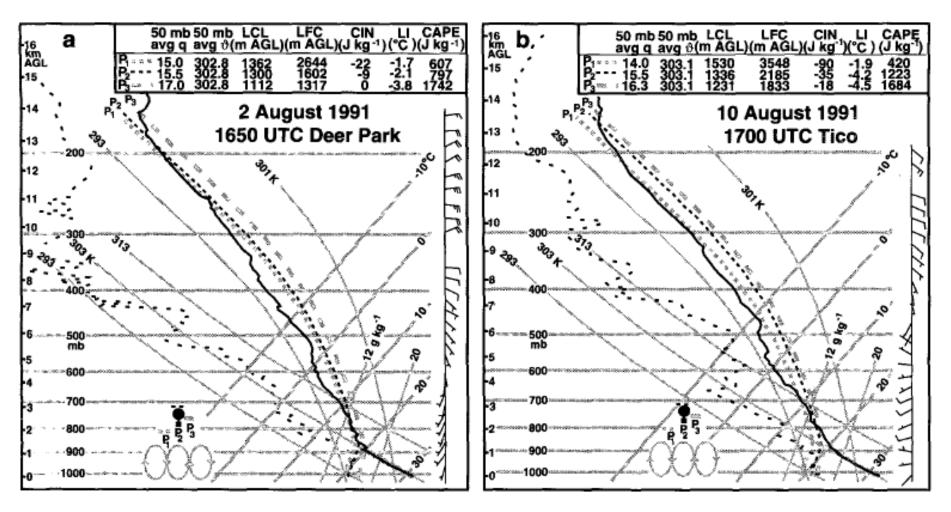


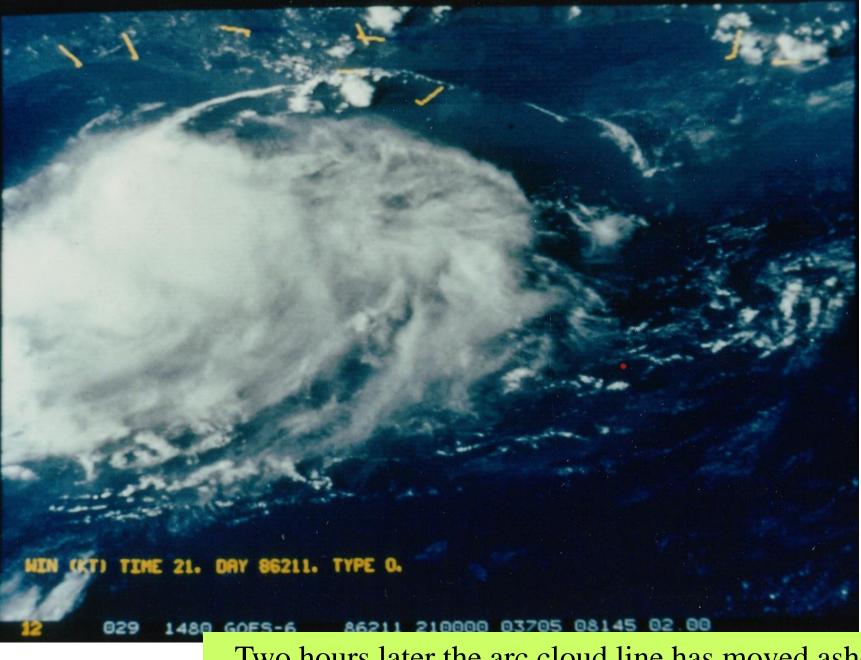
FIG. 9. Full soundings for (a) 1650 UTC 2 August of Fig. 8a and (b) 1700 UTC 10 August of Fig. 8b. Three parcel ascent tracks are shown to indicate the variations depending on low-level mixing ratio values. Parcel 1 (P_1) represents the minimum moisture measured by the aircraft, P_2 represents the parcel ascents expected from the soundings, and P_3 represents both the maximum moisture measured by the aircraft and the parcels producing cloud-base heights determined from photogrammetry. Tables showing stability parameters for the three parcel ascents are shown. Wind barbs are the same as in Fig. 5.

Differences in moisture dominate the convective potential.



Notice how well the arc shaped outflow line is defined. Ahead of the line to the North small areas of convection are developing over land near upper picture center (around the wind barbs)

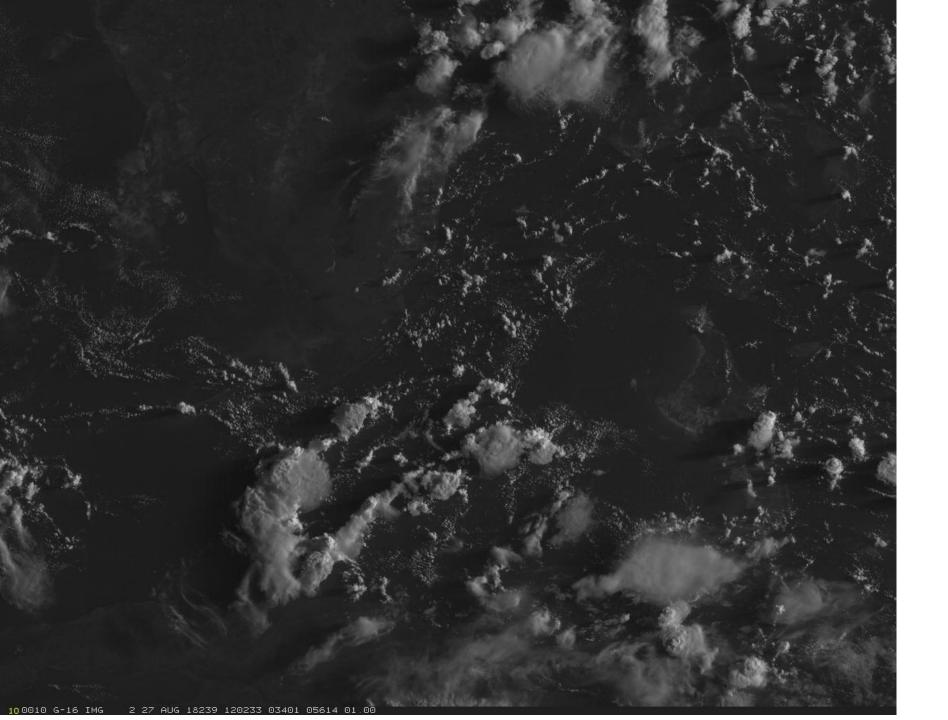
Arc cloud line moving northward from a large convective region over the Gulf of Mexico



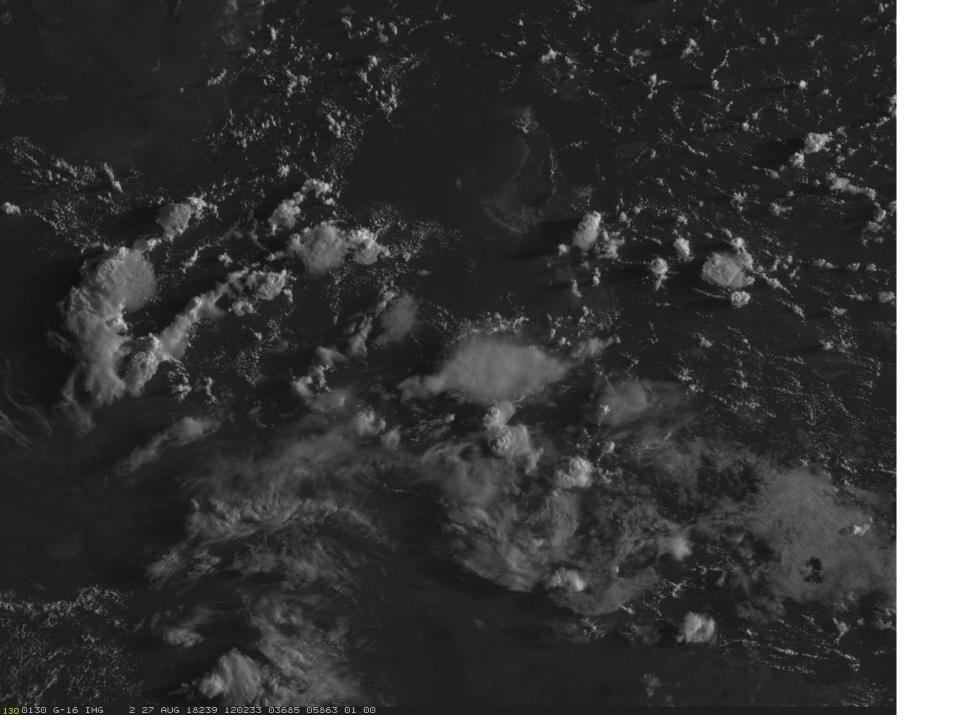
Notice the arc shaped outflow line is still observed but has decreased in cloudiness as it spread out into the Northern Gulf of Mexico (forcing along it has decreased except where its vertical motion has interacted with the convective cloudiness that was developing over land). Vorticity generated due to differential heating has played a key role in holding the arc cloud line together as it moved northward.

A clear example of convective scale interaction driving the development and evolution of thunderstorm activity under weak synoptic forcing.

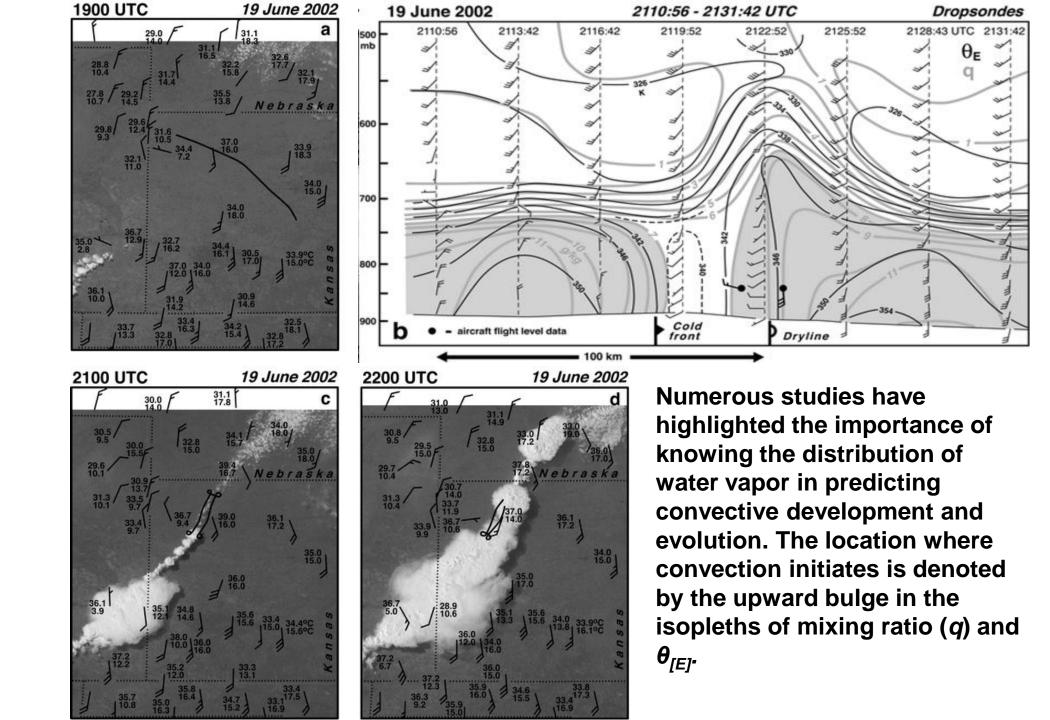
Two hours later the arc cloud line has moved ashore triggering new convection (in preferred locations).



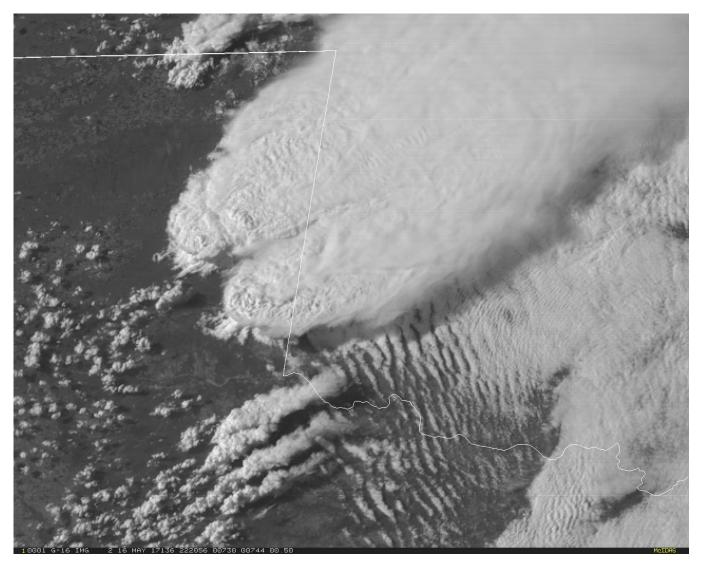
Convective cloud movement over the ocean South of Florida, 27 August 2018 at 5 minute intervals. Try and follow the evolution of the cloud field – fairly easy to do if concentrate on one small area.



Convective cloud movement over the ocean South of Florida, 27 August 2018 at 5 minute intervals in cloud relative animation mode. Try and follow the evolution of the cloud field – fairly easy to do since mean cloud movement has been removed. Notice the stability of the cloud lines and the development and subsequent demise of convection on those lines. These small outflow boundaries provide stability to the cloud line circulation system – with lack of strong friction the rotation in the lines lead to their longer life times, awaiting their interaction with other cloudy regions for longevity.



We've moved to 5-10 minute global imaging with the possibility of 30 second to 1 minute interval rapid scanning of mesoscale sectors



One minute interval visible loop Organized circulation Vorticity - On the local scale

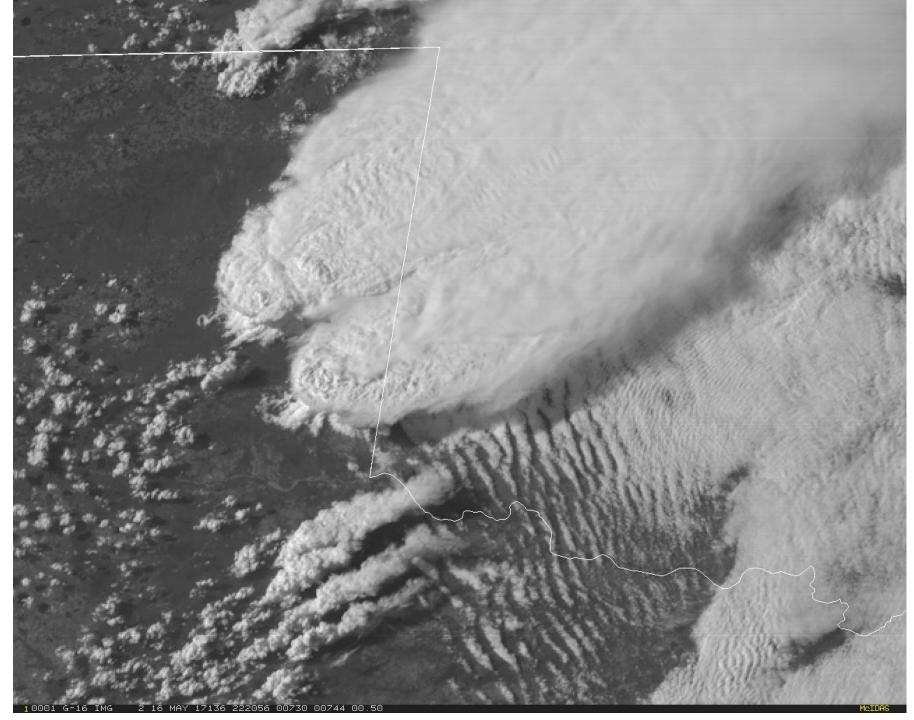
- Convergence on preexisting vorticity
- Tilting of vorticity from one plane to another
- Advection from one place to another
- Differential heating (does not require pre-existing vorticity)
- Friction



Two things to note in this animation.

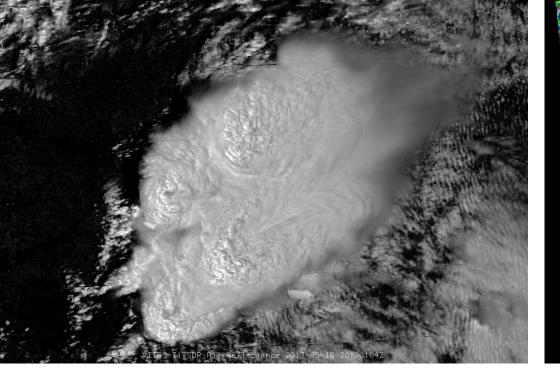
- The cloud streets moving Northward in the loop appear to be almost rolling, which actually is a reflection of shear across that stably capped cloud street layer (water clouds).
- 2) Inspect of the North most storm at the beginning of the animation: as it evolves the cloud streets can be seen being "tilted" upward into the storm due to increasing vertical motion and buoyancy.

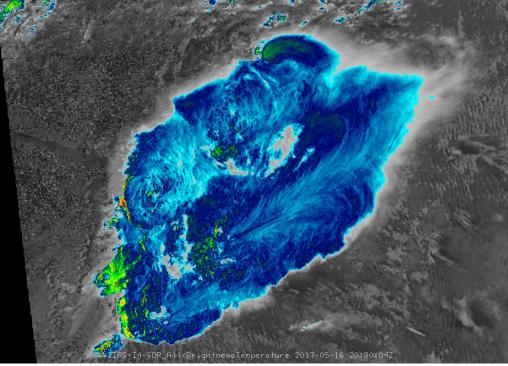
(dw	дu	_	дw	$\frac{\partial v}{\partial v}$
(dy	∂z		∂x	∂z

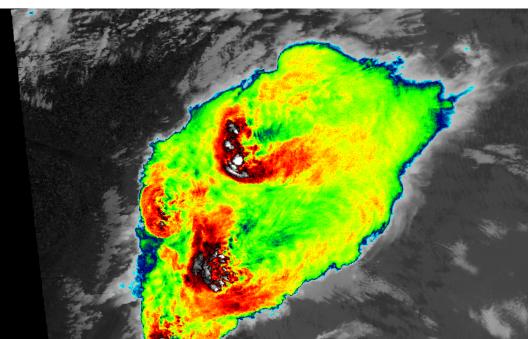


One minute interval visible loop illustrating that In organized strong convection the tilting of vorticity from one plane into another can have a dramatic effect on a thunderstorm's development and severity.

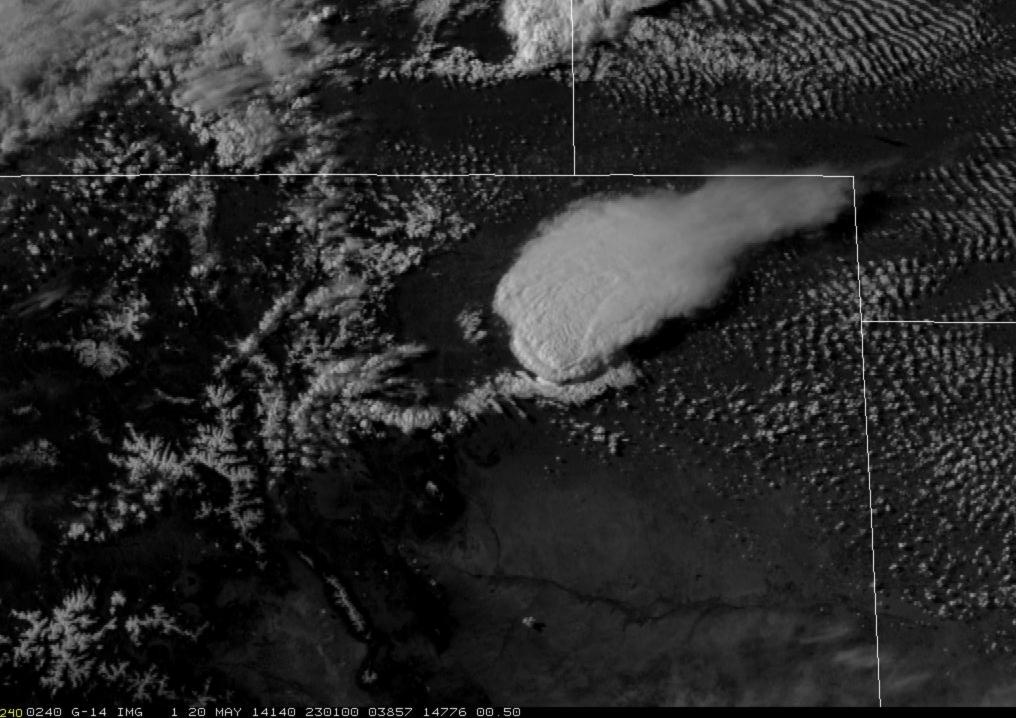
Notice the smooth plumes that are downwind from the overshooting top area.



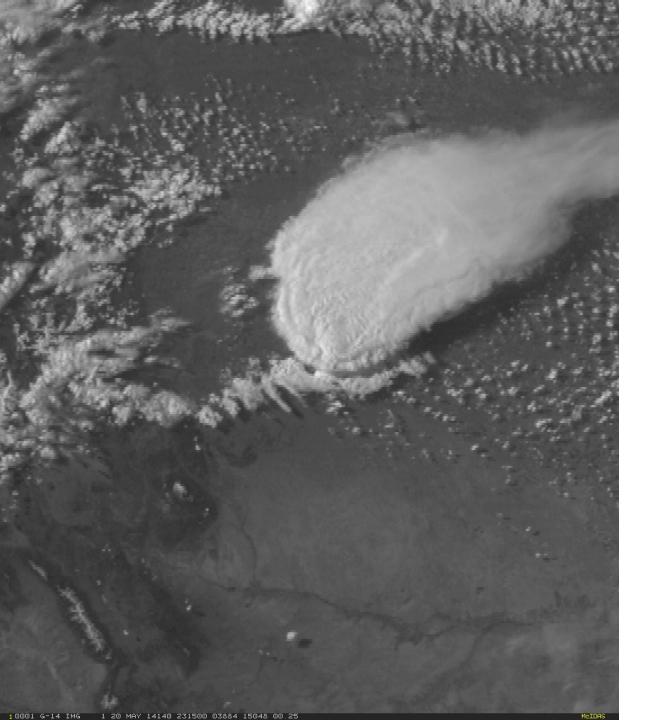




VIIRS Visible (top left) enhanced 3.9 micron (top right) and enhanced 10.3 micron (bottom left). These images are a few hours prior to the animations shown above, but note the characteristics of the downwind above anvil plume from the overshooting top area which is distinctly colder (white regions enclosed within black and red areas). Note the plume area in this example is warmer (green in 10.3 micro) and brighter (blueish white in 3.9 micon).

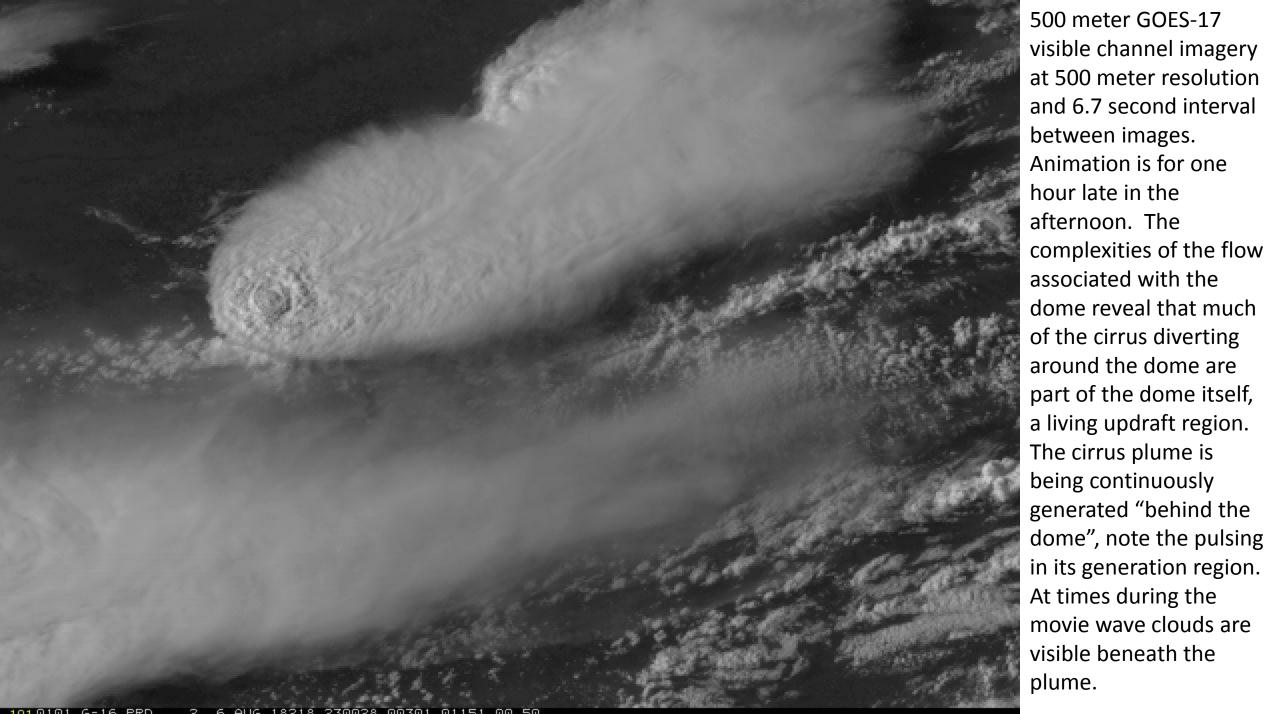


One minute interval animation of severe storm over Northeast Colorado on the afternoon of May 20, 2014. The loop period is about one hour. Notice the smooth plumes extending downwind from the storm overshooting top area.

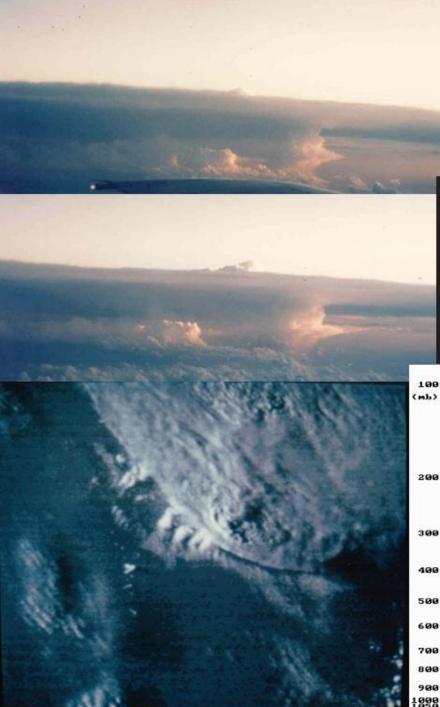


Zoom in of 20 May 2014 storm with about a 20 minute animation and in a storm relative mode (storm overshooting dome is center point of movie (notice how the ground moves, not the storm allowing you to study storm top behavior in greater detail)).

Of note here are the small waves downwind of the anvil that are in the apparent plume generation region as well as the domes apparent pushing back against the ambient flow with anvil cirrus going around the dome on either side of it.

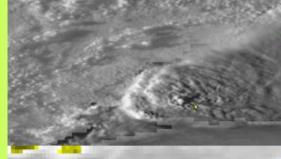


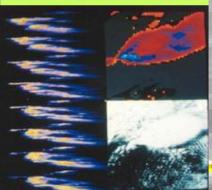
6 AUG 18218 230028 00301 01151 00.50 1010101 G-16 PRD



R 79101 001500 03067 11412 00.50

Storm cloud top structure as a proxy for severe weather and heavy rainfall





// GRI Eta ana

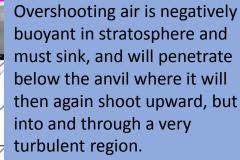
10090121 .GRI

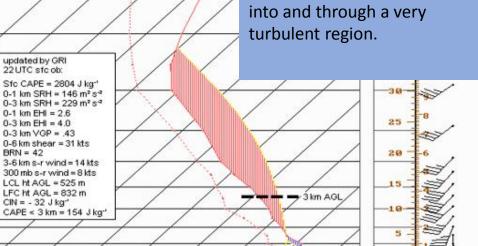
storm motion estimate 227* 26kts

-30

-20

-10





10

We've been looking at this storm top structure (smooth cirrus downwind from anvil, many times a difference in anvil temperature often called a "v notch" with colder anvil top along the legs of the "v notch" with warmer downstream from the overshooting top, and that is very very (almost always) associated with a severe storm (hail, tornadoes or damaging wind). The question has been why the downstream, near continuous smooth cirrus plume above the anvil (which is many times warmer (but will depend on the tropopause structure)). It's associated with a continuous intense updraft that penetrates into the stratosphere, that doesn't collapse but rather interacts with environment acting much like an obstacle to the ambient flow, but one with buoyancy and its own flow to take into account.



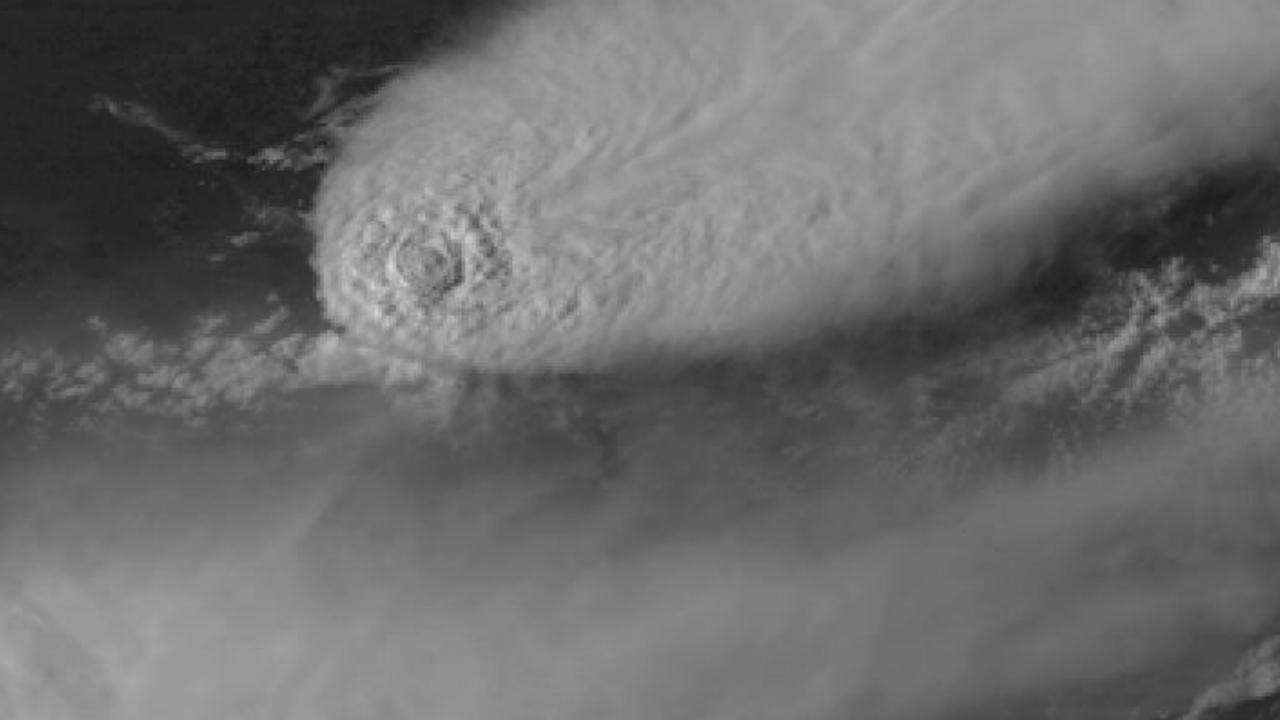
Expansion of the 6.7 second GOES-17 animation and that of a rock embedded in a stream flow. Notice the turbulent region on the downflow side of the rock. Similar, but not exactly the same things occur downstream from the overshooting top region of many severe thunderstorms, but depend on atmospheric tropopause structure and anvil level wind flow relative to the thunderstorm updraft as it penetrates into the stratosphere.

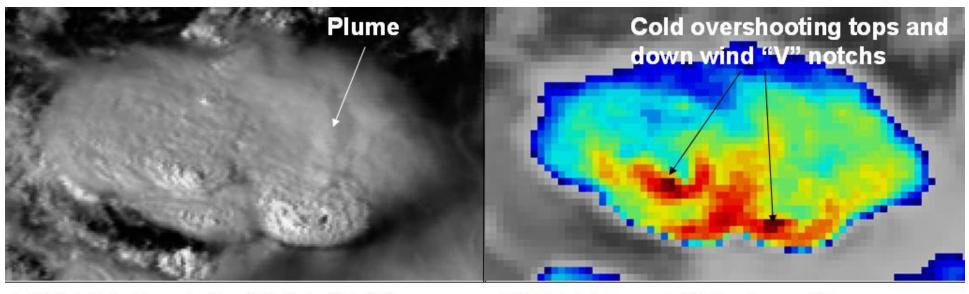




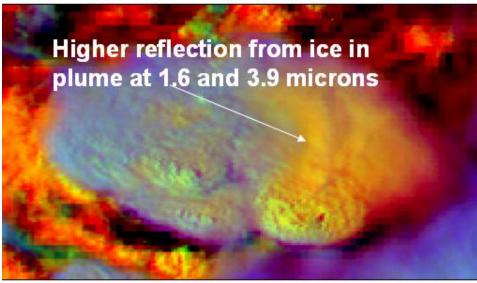
Expansion of the 6.7 second GOES-17 animation and that of a rock embedded in a stream flow. Notice the turbulent region on the downflow side of the rock. Above the turbulent structure dynamics similar to those that form the altocumulus standing lenticularis cloud form provide a mechanism that allow for the ice crystals from overshooting top which have descended into the anvil area only to become positively buoyant once again and ascend through the turbulent region. Unlike the acsl cloud (as above) the mechanism id fed with small ice crystals which are long lived.







MSG High Resolution Visible (HRV)



MSG 3 channel color image using HRV, 1.6 and 3.9 micron channel data

MSG Enhanced 10.7 micron IR

Figure 27: Thunderstorm tops over Europe from MSG on 29 July 2005 at 14:30 UTC. This case, presented by Martin Sevtak at the EUMETSAT Users' Conference showed higher reflection from ice in the plume at thunderstorm top in 1.6 and 3.9 microns, likely due to smaller cloud particle size and related to updraft characteristics. Cold overshooting top and "V" notches are clearly shown in the 10.7 channel image, as are the plume brighter reflection from the right-most storm.

So, what of our new capabilities with these new satellites? A confirmation of some old with some new insights.

- Vorticity on the local scale is of exceptional importance in the organization, development and evolution of deep convection from differential heating mechanisms as land/sea breezes to more complicated interactions related to the development of thunderstorm outflow boundaries and those boundaries interactions with local cumulus and clear regions.
- In organized strong convection the tilting of vorticity from one plane into another can have a dramatic effect on a thunderstorm's development and severity.
- Well defined above anvil plumes downwind from a thunderstorm's overshooting top are an indicator of a long lived "supercell" type storm. They are similar to an altocumulus standing lenticularis cloud (acsl) mechanism mechanism wise, but also reflect the result of the storm's continuous updraft characteristics coupled with strong turbulence and mixing downwind of the overshooting area. Unlike the acsl, this cloud is composed of ice crystals which do not evaporate in the "trough" of the wave generation mechanism, That the plume can extend for long distances and its

So, what of our new capabilities with these new satellites? A confirmation of some old with some new insights.

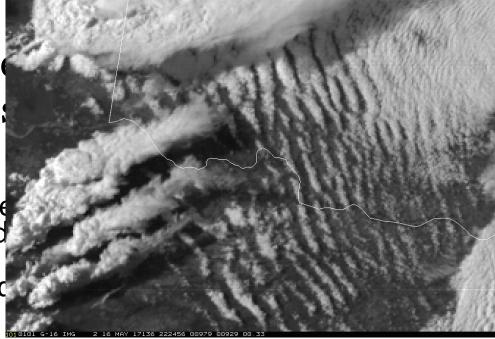
- Vorticity on the local scale is of exceptional importance in the organization, development and evolution of deep convection from differential heating mechanisms as land/sea breezes to more complicated interactions related to the development of thunderstorm outflow boundaries and those boundaries interactions with local cumulus and clear regions.
- In organized strong convection the tilting of vorticity 1 can have a dramatic effect on a thunderstorm's devel
- Well defined above anvil plumes downwind from a th are an indicator of a long lived "supercell" type storm the storm's continuous updraft characteristics couple mixing downwind of the overshooting area. That the distances as a continuous plume speaks to the longev mechanisms.



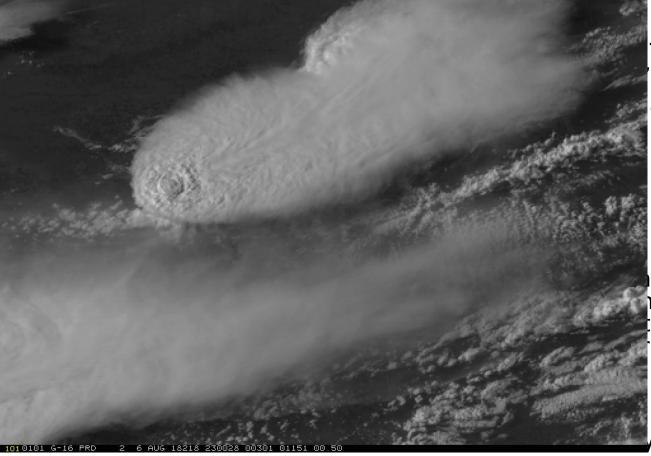
July 13th edition

So, what of our new capabilities satellites? A confirmation of a new insights.

 Vorticity on the local scale is of exceptional importance development and evolution of deep convection from d mechanisms as land/sea breezes to more complicated development of thunderstorm outflow boundaries and interactions with local cumulus and clear regions.



- In organized strong convection the tilting of vorticity from one plane into another can have a dramatic effect on a thunderstorm's development and severity.
- Well defined above anvil plumes downwind from a thunderstorm's overshooting top are an indicator of a long lived "supercell" type storm. They are likely the result of the storm's continuous updraft characteristics coupled with strong turbulence and mixing downwind of the overshooting area. That the plume can extend for long distances as a continuous plume speaks to the longevity of its generating mechanisms.



bilities with these new on of some old with some ights.

ice in the organization, development and ng mechanisms as land/sea breezes to more of thunderstorm outflow boundaries and those regions.

from one plane into another can have a dramatic

Well defined above anvil plumes downwind from a thunderstorm's overshooting top are an indicator
of a long lived "supercell" type storm. They are likely the result of the storm's continuous updraft
characteristics coupled with strong turbulence and mixing downwind of the overshooting area. That
the plume can extend for long distances as a continuous plume speaks to the longevity of its
generating mechanisms. Upwind the storm's continuous updraft spreads out into the flow causing
blocking as in normal flow around an obstacle (local high pressure and diversion around the updraft
region) while downwind it adds its velocity to the ambient flow causing a lowering of pressure as it
sinks beneath the anvil only to reemerge into an exceptionally turbulent region where it mixes with
that cloudy air and again overshoots providing a source of smaller ice particles (likely in part due to
collision with ice particles within the turbulent region) in the stratosphere where a downstream cloud
generation mechanism similar to that for altocumulus standing lenticularis awaits their arrival.